```
#include <stdlib.h>
#include <stdio.h>
#include <math.h>
/* This code is a translation of Norvig's (1992) LISP implementation,
though it deviates from it in several respects. In theory you might be
able to track down this code and turn much of it in to satisfy the
project requirements, but consistent with the honor code (and ethics
generally), you would declare this use and would receive a MUCH
reduced grade.
```

Douglas H. Fisher
*/
/* How to play the Game of Othello
Othello is a game between two players on an $8 \times 8$ square grid (64 positions). The two players, represented as black (b) and white (w), initially occupy the center positions as indicated below.

12345678
1
2
. . . .
-•••••
4 . . . W b . . .
5 . . . b w . . .
6 . . . . . . . .
7 . . . . . . . .
8 . . . . . . . .

Black moves first, and places a 'b' somewhere on an *empty* location (indicated by a '.'). There are constraints on where the b may be placed though (other than 'empty'). Notably, the b must be placed so that it brackets or sandwiches a contiguous sequence of opponent pieces. So, a b can be placed at coordinates (3,4), (4,3), $(5,6)$,
or $(6,5)$. When $a b$ is placed that causes a sequence of ws to be bracketed,
the ws that are bracketed are flipped to b (i.e., from the opponent's
color to the current player's color). So, placing a 'b' at (5,6) leads to the following board:

12345678

```
6
7
8
```

White now moves. Any move must bracket at least one b piece, and after doing so, the bs in the bracketed sequence are switched to ws. For the board above, w could be placed on (6,4), $(4,6)$, or $(6,6)$-- note that one can bracket pieces along a diagnoal. If w is placed on $(6,6)$, the resulting board is:

12345678
5 . . . b w b . .
6 . . . . . W . .
7 . . . . . . . .
8 . . . . . . . .

Play continues:
12345678
b to $(4,3)$

1
2 3 4 5 . . . b w b . . 6 . . . . . W . . 7 8

$$
12345678 \quad \text { w to }(5,3)
$$

$$
1
$$

3 . . . . . . . .
4 . . b b b . . .
5 . . w w w b . .
6 . . . . . W . .
7 . . . . . . .
8 . . . . . . . .
$12345678 \quad b$ to $(6,5)$. Notice that this brackets
1
2
3
$\begin{array}{lll}\text {. . . . . . . . } & \text { a white piece along a vertical AND diagonal } \\ \text {. . . . . . . . } & \text { path, causing both sequences to be switched } \\ \text {. . . . . . . . } \\ \text {. } & \text { b b }\end{array}$

```
5 . . w b b b . .
6 . . . . b w . .
7 . . . . . . . .
8 . . . . . . . .
```

$12345678 \quad w$ to $(3,3)$. Again, this brackets $b$ along 1 two sequences. In general, all bracketed sequences (there may by many) are

4 . . w w b . . .
5 . . w b w b . .
6 . . . . b w . .
7 . . . . . . .
8 . . . . . . . .
Play continues until neither player can move. Very often, this happens when all sqaures are filled, but both players may be unable to bracket a sequence of opponents' pieces before all squares are filled, and so the game stops before all squares are filled. The player with the most squares filled at game's end, wins.

If one player cannot move (because they cannot bracket an opposing sequence), but the other player can move, then the former player must pass until such time that they can move.

Note that when running the program, where one of the players is human, a board will be printed as follows:

12345678


10 20 30 40 60 . . . . b w . . 70 . . . . . . . . 80 . . . . . . . .

Specify a move by the sum of the appropriate row and column. So, for example, 42 would be a legal move for black. If you specify an illegal move (e.g., 23 in this example), you will . . . . . . . $\quad$ Specify a move by the sum of
. . . . . . . . . row and column. So, for examp
. . w w b . . . . $\quad$ legal move for black. If you
. . w b w b . . .
. be prompted for another move.
$/ * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * *$ $* * * * * * * * * * * * * * * * * * * * *$ GLOBAL VARS and CONSTANTS $* * * * * * * * * * * * * * * * * *$ $* * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * * /$
/* global variables and constants are given in all CAPS */ const int ALLDIRECTIONS[8]=\{-11, $-10,-9,-1,1,9,10,11\} ;$ const int BOARDSIZE=100;

```
/* Each array/board position can have one of 4 values */
const int EMPTY=0;
const int BLACK=1;
const int WHITE=2;
const int OUTER=3; /* the value of a square on the perimeter
*/
const int WIN=2000; /* a WIN and LOSS for player are outside
*/
const int LOSS= -2000; /* the range of any board evaluation
function */
```

/* the global variable, BOARDS, is used to count the number of BOARDS examined during minmax search (and is printed during a roundrobin tournament). See the end of this file for sample results of roundrobin tournaments.
*/
long int BOARDS;
/* STRATEGIES is an array of strategy names (for printing) and pointers to the functions that implement each strategy. It is the only structure/statement/function that must be modified when a new strategy is added (other than adding the actual function(s) that implements a new strategy.
int human (int, int *);
int randomstrategy(int, int *);
int maxdiffstrategy1(int, int *);
int maxdiffstrategy3(int, int *);
int maxdiffstrategy5(int, int *);
int maxweighteddiffstrategy1(int, int *);
int maxweighteddiffstrategy3(int, int *);
int maxweighteddiffstrategy5(int, int *);
void * STRATEGIES[9][4] = \{
\{"human", "human", human\},
\{"random", "random", randomstrategy\},
\{"diff1", "maxdiff, 1-move minmax lookahead", maxdiffstrategy1\},
\{"diff3", "maxdiff, 3-move minmax lookahead", maxdiffstrategy3\},
\{"diff5", "maxdiff, 5-move minmax lookahead", maxdiffstrategy5\},
\{"wdiff1", "maxweigteddiff, 1-move minmax lookahead",
maxweighteddiffstrategy1\},
\{"wdiff3", "maxweigteddiff, 3-move minmax lookahead",
maxweighteddiffstrategy3\},
\{"wdiff5", "maxweigteddiff, 5-move minmax lookahead",
maxweighteddiffstrategy5\}, \{NULL, NULL, NULL\} \};

```
typedef int (* fpc) (int, int *);
/
**********************************************************************
*/
/*************************** Auxiliary Functions
****************************/
/
**********************************************************************
*/
/* the possible square values are integers (0-3), but we will
        actually want to print the board as a grid of symbols, . instead of
0,
    b instead of 1, w instead of 2, and ? instead of 3 (though we
    might only print out this latter case for purposes of debugging).
*/
char nameof (int piece) {
    static char piecenames[5] = ".bw?";
    return(piecenames[piece]);
}
/* if the current player is BLACK (1), then the opponent is WHITE (2),
        and vice versa
*/
int opponent (int player) {
    switch (player) {
    case 1: return 2;
    case 2: return 1;
    default: printf("illegal player\n"); return 0;
    }
}
```

/* The copyboard function mallocs space for a board, then copies
the values of a given board to the newly malloced board.
*/
int * copyboard (int * board) \{
int i, * newboard;
newboard $=($ int $*)$ malloc (BOARDSIZE $*$ sizeof(int));
for (i=0; i<BOARDSIZE; i++) newboard[i] = board[i]; return newboard;
\}

```
/* the initial board has values of 3 (OUTER) on the perimeter,
    and EMPTY (0) everywhere else, except the center locations
    which will have two BLACK (1) and two WHITE (2) values.
*/
int * initialboard (void) {
    int i, * board;
    board = (int *)malloc(BOARDSIZE * sizeof(int));
    for (i = 0; i<=9; i++) board[i]=OUTER;
    for (i = 10; i<=89; i++) {
        if (i%10 >= 1 && i%10 <= 8) board[i]=EMPTY; else board[i]=OUTER;
    }
    for (i = 90; i<=99; i++) board[i]=OUTER;
    board[44]=WHITE; board[45]=BLACK; board[54]=BLACK; board[55]=WHITE;
    return board;
}
```

/* count the number of squares occupied by a given player (1 or 2,
or alternatively BLACK or WHITE)
*/
int count (int player, int $*$ board) \{
int i, cnt;
cnt=0;
for ( $i=1$; $i<=88$; $i++$ )
if (board[i] == player) cnt++;
return cnt;
\}
/* The printboard routine does not print "OUTER" values of the array, since these are not squares of the board. Rather it examines all other locations and prints the symbolic representation (.,b,w) of each board square. So the initial board would be printed as follows:

12345678 [b=2 w=2]

```
70 . . . . . . . .
80 . . . . . . . .
Notice that if you add row, r, and column, c, numbers, you
get the array location that corresponds to (r,c). So
square (50,6) corresponds to 50+6=56.
*/
void printboard (int * board) {
    int row, col;
    printf(" 1 2 3 4 5 6 7 8 [%c=%d %c=%d]\n",
        nameof(BLACK), count(BLACK, board), nameof(WHITE), count(WHITE,
board));
    for (row=1; row<=8; row++) {
            printf("%d ", 10*row);
            for (col=1; col<=8; col++)
                printf("%c ", nameof(board[col + (10 * row)]));
            printf("\n");
    }
}
/
****************************************************************************
*
********************** Routines for insuring legal play
*****************
**********************************************************************
*/
/*
The code that follows enforces the rules of legal play for Othello.
*/
/* a "valid" move must be a non-perimeter square */
int validp (int move) {
    if ((move >= 11) && (move <= 88) && (move%10 >= 1) && (move%10 <=
8))
            return 1;
    else return 0;
}
/* findbracketingpiece is called from wouldflip (below). findbracketingpiece starts from a *square* that is occupied by a *player*'s opponent, moves in a direction, *dir*, past all opponent pieces, until a square occupied by the \(*\) player*
```

is found. If a square occupied by *player* is not found before hitting an EMPTY or OUTER square, then 0 is returned (i.e., no bracketing piece found). For example, if the current board is

12345678

10
20
30
40
50
60
70
80

then findbracketingpiece(66, BLACK, board, -11) will return 44 findbracketingpiece(53, BLACK, board, 1) will return 56 findbracketingpiece(55, BLACK, board, -9) will return 0

```
*/
```

int findbracketingpiece(int square, int player, int * board, int dir) \{
while (board[square] == opponent(player)) square = square + dir;
if (board[square] == player) return square;
else return 0;
\}
/* wouldflip is called by legalmove (below). Give a *move* (square)
to which a player is considering moving, wouldflip returns
the square that brackets opponent pieces (along with the sqaure
under consideration, or 0 if no such bracketing square exists
*/
int wouldflip (int move, int player, int $*$ board, int dir) \{
int c;
c = move + dir;
if (board[c] == opponent(player))
return findbracketingpiece(c+dir, player, board, dir);
else return 0;
\}
/* A "legal" move is a valid move, but it is also a move/location that will bracket a sequence of the opposing player's pieces, thus flipping at least one opponent piece. legalp considers a move/square and seaches in all directions for at least one
bracketing
square. The function returns 1 if at least one bracketing square is found, and 0 otherwise.

```
*/
int legalp (int move, int player, int * board) {
    int i;
    if (!validp(move)) return 0;
    if (board[move]==EMPTY) {
        i=0;
        while (i<=7 && !wouldflip(move, player, board, ALLDIRECTIONS[i]))
i++;
        if (i==8) return 0; else return 1;
    }
    else return 0;
}
```

/* makeflips is called by makemove. Once a player has decided
on a move, all (if any) opponent pieces that are bracketed
along a given direction, dir, are flipped.
*/
void makeflips (int move, int player, int * board, int dir) \{
int bracketer, c;
bracketer = wouldflip(move, player, board, dir);
if (bracketer) \{
c = move + dir;
do \{
board [c] = player;
c = c + dir;
\} while (c != bracketer);
\}
\}
/* makemove actually places a players symbol (BLACK or WHITE)
in the location indicated by move, and flips all opponent
squares that are now bracketed (along all directions)
*/
void makemove (int move, int player, int * board) \{
int i;
board[move] = player;
for (i=0; i<=7; i++) makeflips(move, player, board,
ALLDIRECTIONS[i]);
\}
/* anylegalmove returns 1 if a player has at least one legal
move and 0 otherwise. It is called by nexttoplay (below)
*/

```
int anylegalmove (int player, int * board) {
    int move;
    move = 11;
    while (move <= 88 && !legalp(move, player, board)) move++;
    if (move <= 88) return 1; else return 0;
}
```

/* choose the player with the next move. Typically this will be the player other than previousplayer, unless the former has no legal move available, in which case previousplayer remains the current player. If no players have a legalmove available, then nexttoplay returns 0. */
int nexttoplay (int * board, int previousplayer, int printflag) \{ int opp;
opp = opponent(previousplayer);
if (anylegalmove(opp, board)) return opp;
if (anylegalmove(previousplayer, board)) \{ if (printflag) printf("\%c has no moves and must pass.\n", nameof(opp)); return previousplayer;
\}
return 0; \}
/* if a machine player, then legalmoves will be called to store all the current legal moves in the moves array, which is then returned.
moves[0] gives the number of legal moves of player given board. The legal moves (i.e., integers representing board locations) are stored in moves[1] through moves[moves[0]].
*/
int * legalmoves (int player, int * board) \{
int move, i, * moves;
moves $=(i n t *) m a l l o c(65 * \operatorname{sizeof(int));~}$
moves[0] = 0;
i = 0;
for (move=11; move<=88; move++) if (legalp(move, player, board)) \{
i++;
moves[i]=move;
\}
moves[0]=i;
return moves;
\}

```
/* if a human player, then get the next move from standard input */
int human (int player, int * board) {
    int move;
    printf("%c to move:", nameof(player)); scanf("%d", &move);
    return move;
}
```

/* a random machine strategy chooses randomly among the
legal available moves.
*/
int randomstrategy(int player, int * board) \{
int r, * moves;
moves = legalmoves(player, board);
$r=\operatorname{moves}[(\operatorname{rand}() \%$ moves[0]) +1$]$;
free(moves);
return(r);
\}
/*
int randomstrategy(int player, int * board) \{
static int i=0;
int $r$, * moves;
moves = legalmoves(player, board);
$r=$ moves[(i \% moves[0]) +1$]$;
i++;
free(moves);
return(r);
\}
*/
/* diffeval and weighteddiffeval are alternate utility functions
for evaluation the quality (from the perspective of player)
of terminal boards in a minmax search.
*/
int diffeval (int player, int * board) \{ /* utility is measured */
int i, ocnt, pcnt, opp; /* by the difference in $* /$
pcnt=0; ocnt = 0; /* number of pieces $* /$
opp = opponent(player);
for ( $i=1$; $i<=88$; $i++$ ) \{

```
        if (board[i]==player) pcnt++;
        if (board[i]==opp) ocnt++;
    }
    return (pcnt-ocnt);
}
```

/* some machine strategies will regard some squares as more important
than others. The goodness of a square/move is given by a weight.
Every
perimeter square will have importance 0. Corner squares are the
"best" squares to obtain. Why? Negative weights indicate that a
square should be avoided. Why are weights of certain squares
adjacent to
corners and certain edges negative? The weights array gives the
importance of each square/move.
*/
int weighteddiffeval (int player, int * board) \{
int i, ocnt, pcnt, opp;
const int weights[100]=\{0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
$0,120,-20,20,5,5,20,-20,120,0$,
$0,-20,-40,-5,-5,-5,-5,-40,-20,0$,
$0,20,-5,15,3,3,15,-5,20,0$,
$0,5,-5,3,3,3,3,-5,5,3$,
$0,5,-5,3,3,3,3,-5,5,3$,
$0,20,-5,15,3,3,15,-5,20,0$,
$0,-20,-40,-5,-5,-5,-5,-40,-20,0$,
$0,120,-20,20,5,5,20,-20,120,0$,
$0,0,0,0,0,0,0,0,0,0\}$;
pcnt=0; ocnt=0;
opp = opponent(player);
for (i=1; i<=88; i++) \{
if (board[i]==player) pcnt=pcnt+weights[i];
if (board[i]==opp) ocnt=ocnt+weights[i];
\}
return (pcnt - ocnt);
\}
/* minmax is called to do a "ply" move lookahead, using evalfn (i.e., the utility function) to evaluate (terminal) boards at the end of lookahead. Minmax starts by finding and simulating each legal
move by player. The move that leads to the best (maximum backed-up score)
resulting board, is the move (i.e., an integer representing a board location) that is returned by minmax.
The score of each board (resulting from each move)
is determined by the function diffeval if no player can move from the resulting board (i.e., game over), by function maxchoice if only player can move from the resulting board, or by function minchoice if the opponent can move from the resulting board.

Importantly, minmax assumes that ply >= 1 .
You are to modify minmax so that it exploits alphabeta pruning, and so that it randomly selects amongst the best moves for player.

```
*/
```

int minmax (int player, int * board, int ply, int (* evalfn) (int, int *) ) \{
int i, max, ntm, newscore, bestmove, * moves, * newboard;
int maxchoice (int, int $*$, int, int (*) (int, int *)); int minchoice (int, int $*$, int, int (*) (int, int *)); moves $=$ legalmoves(player, board); /* get all legal moves for player */
max = LOSS - 1; /* any legal move will exceed this score */
for (i=1; i <= moves[0]; i++) \{ newboard = copyboard(board); BOARDS = BOARDS + 1; makemove(moves[i], player, newboard); ntm = nexttoplay(newboard, player, 0); if (ntm == 0) \{ /* game over, so determine winner */
newscore = diffeval(player, newboard);
if (newscore > 0) newscore = WIN; /* a win for player */
if (newscore < 0) newscore = LOSS; /* a win for opp */ \}
if (ntm == player) /* opponent cannot move */
newscore $=$ maxchoice(player, newboard, ply-1, evalfn);
if (ntm == opponent(player))
newscore = minchoice(player, newboard, ply-1, evalfn);
if (newscore > max) \{
max = newscore;
bestmove = moves[i]; /* a better move found */
\}
free(newboard);
\}
free(moves);
return(bestmove);
\}
/* If ply = 0, then maxchoice should return diffeval(player, board), else the legal moves that can be made by player from board should be simulated. maxchoice should return the MAXIMUM board score
from among the possibilities. The backed-up score of each board (resulting from each player move) is determined by function maxchoice if only player can move from the resulting board,
by function minchoice if the opponent can move from the resulting board,
is WIN if a win for player, a LOSS if a win for opponent, and a 0 if a draw.

If two or more boards tie for the maximum backed score, then return the move that appears first (lowest location) in the moves array leading to a maximum-score board.

```
*/
int maxchoice (int player, int * board, int ply,
                    int (* evalfn) (int, int *)) {
    int i, max, ntm, newscore, * moves, * newboard;
    int minchoice (int, int *, int, int (*) (int, int *));
    if (ply == 0) return((* evalfn) (player, board));
    moves = legalmoves(player, board);
    max = LOSS - 1;
    for (i=1; i <= moves[0]; i++) {
        newboard = copyboard(board); BOARDS = BOARDS + 1;
        makemove(moves[i], player, newboard);
        ntm = nexttoplay(newboard, player, 0);
        if (ntm == 0) {
            newscore = diffeval(player, newboard);
            if (newscore > 0) newscore = WIN;
            if (newscore < 0) newscore = LOSS;
        }
        if (ntm == player)
            newscore = maxchoice(player, newboard, ply-1, evalfn);
        if (ntm == opponent(player))
            newscore = minchoice(player, newboard, ply-1, evalfn);
        if (newscore > max) max = newscore;
        free(newboard);
    }
    free(moves);
    return(max);
}
```

/* If ply $=0$, then minchoice should return the diffeval(player, board),
else the legal moves that can be made by player's opponent from board should be simulated. minchoice should return the MINIMUM backed up board score
from among the possibilities. The backed up score of each board
(resulting from each opponent move) is determined by function maxchoice
if player can move from the resulting board,
by function minchoice if only the opponent can move from the resulting board, is WIN if a win for player, a LOSS if a win for opponent, and a 0 if a draw.

If two or more BOARDS tie for the minimum score, then return the move that appears first (lowest location) in the moves array leading to a minimum-score board.

Advanced: DO NOT worry about this, but note that minchoice and maxchoice could be combined easily into a single function, finding the board with minimum score, $s$, is equivalent to finding the board with maximum $-1 * s$. One would have to add an additional parameter to decide whether to multiply by a -1 factor or not in computing a board score in this combined function. With a bit more work, one could combine all three functions, minmax, maxchoice, and minchoice, into a single function.

```
*/
```

int minchoice (int player, int * board, int ply, int (* evalfn) (int, int *)) \{ int i, min, ntm, newscore, * moves, * newboard;
if (ply == 0) return((* evalfn) (player, board));
moves = legalmoves(opponent(player), board);
min = WIN+1;
for (i=1; i <= moves[0]; i++) \{
newboard = copyboard(board); BOARDS = BOARDS + 1;
makemove(moves[i], opponent(player), newboard);
ntm = nexttoplay(newboard, opponent(player), 0);
if (ntm == 0) \{
newscore = diffeval(player, newboard);
if (newscore > 0) newscore = WIN;
if (newscore < 0) newscore = LOSS;
\}
if (ntm == player)
newscore = maxchoice(player, newboard, ply-1, evalfn);
if (ntm == opponent(player))
newscore = minchoice(player, newboard, ply-1, evalfn);
if (newscore < min) min = newscore;
free(newboard);
\}
free(moves);
return(min);
\}

```
/* the following strategies use minmax search, in contrast to
randomstrategy
*/
int maxdiffstrategy1(int player, int * board) { /* 1 ply lookahead */
    return(minmax(player, board, 1, diffeval)); /* diffeval as utility
fn */
}
int maxdiffstrategy3(int player, int * board) { /* 3 ply lookahead */
    return(minmax(player, board, 3, diffeval));
}
int maxdiffstrategy5(int player, int * board) { /* 5 ply lookahead */
    return(minmax(player, board, 5, diffeval));
}
/* use weigteddiffstrategy as utility function */
int maxweighteddiffstrategy1(int player, int * board) {
    return(minmax(player, board, 1, weighteddiffeval));
}
int maxweighteddiffstrategy3(int player, int * board) {
    return(minmax(player, board, 3, weighteddiffeval));
}
int maxweighteddiffstrategy5(int player, int * board) {
        return(minmax(player, board, 5, weighteddiffeval));
}
/******************************************************************
***************************** Coordinating matches *******************
******************************************************************/
/* get the next move for player using strategy */
void getmove (int (* strategy) (int, int *), int player, int * board,
                int printflag) {
    int move;
    if (printflag) printboard(board);
    move = (* strategy)(player, board);
    if (legalp(move, player, board)) {
        if (printflag) printf("%c moves to %d\n", nameof(player), move);
        makemove(move, player, board);
    }
    else {
```

```
        printf("Illegal move %d\n", move);
        getmove(strategy, player, board, printflag);
    }
}
```

/* the Othello function coordinates a game between two players,
represented by the strategy of each player. The function can
coordinate play between two humans, two machine players, or one of
each.
*/
void othello (int (* blstrategy) (int, int *),
int (* whstrategy) (int, int *), int printflag) \{
int * board;
int player;
board = initialboard();
player = BLACK;
do \{
if (player == BLACK) getmove(blstrategy, BLACK, board, printflag);
else getmove(whstrategy, WHITE, board, printflag);
player = nexttoplay(board, player, printflag);
\}
while (player != 0);
if (printflag) \{
printf("The game is over. Final result:\n");
printboard(board);
\}
\}
/* The following two functions are used for computer player tournaments. Since any pair of non-random strategies will yield exactly the same result from game to game, randomboard is used to introduce some uncertainty/randomness to a game so that different games between the same strategies will yield different results. In particular, randomboard starts with an initialboard, then uses the randomstrategy to make the first 10 moves (5 for each player).
*/
int * randomboard (void) \{
int player, oldplayer, i, * board;
board = initialboard();
player = BLACK;
i=1;
do \{
if (player == BLACK) getmove(randomstrategy, BLACK, board, 0);
else getmove(randomstrategy, WHITE, board, 0);
oldplayer = player;

```
            player = nexttoplay(board, player, 0);
            if (oldplayer == player) {
            free(board);
            return(randomboard());
        }
        i++;
    }
    while (player != 0 && i<=8);
    if (player==0) {
        free(board);
        return(randomboard());
    }
    else return(board);
}
/* Roundrobin pits each known machine strategy found in STRATEGIES
against every other strategy for 10 games, 5 as BLACK and 5 as WHITE.
each game begins with a randomboard. See end of this file for
example outputs of roundrobin.
*/
void roundrobin (void) {
    int i, j, k, cntdiff, player, iwins, jwins, * game1board, *
game2board;
    long int iboards, jboards;
    i=1;
    while (STRATEGIES[i+1][0] != NULL) { /* pit one strategy */
        j = i + 1;
        while (STRATEGIES[j][0] != NULL) { /* against another */
        iwins = 0; jwins = 0; iboards = 0; jboards = 0;
        for (k=1; k<=5; k++) { /* play a strategy as BLACK then as WHITE
*/
                game1board = randomboard(); /* do this 5 times */
                game2board = copyboard(game1board);
                player = BLACK;
                do {
                    if (player == BLACK) {
                    BOARDS = 0;
                    getmove((fpc)STRATEGIES[i][2], BLACK, game1board, 0);
                    iboards = iboards + BOARDS;
                        }
                        else {
                    BOARDS = 0;
                    getmove((fpc)STRATEGIES[j][2], WHITE, game1board, 0);
                    jboards = jboards + BOARDS;
                        }
                        player = nexttoplay(game1board, player, 0);
                }
                while (player != 0);
```

```
            cntdiff = diffeval(BLACK, game1board); /* determine winner */
            if (cntdiff>0) iwins++;
            if (cntdiff<0) jwins++;
            free(game1board);
                player = BLACK;
                do {
            if (player == BLACK) {
                    BOARDS = 0;
                    getmove((fpc)STRATEGIES[j][2], BLACK, game2board, 0);
                    jboards = jboards + BOARDS;
            }
            else {
                        BOARDS = 0;
                    getmove((fpc)STRATEGIES[i][2], WHITE, game2board, 0);
                    iboards = iboards + BOARDS;
            }
            player = nexttoplay(game2board, player, 0);
                }
                while (player != 0);
                cntdiff = diffeval(WHITE, game2board); /* determine winner */
                if (cntdiff>0) iwins++;
                if (cntdiff<0) jwins++;
                free(game2board);
                }
                printf("%s wins=%d boards=%ld || %s wins=%d boards=%ld\n",
                        STRATEGIES[i][0], iwins, iboards,
                        STRATEGIES[j][0], jwins, jboards);
                j++;
        }
        i++;
    }
}
/* playgame interfaces with user to setup a game. Playgame displays
the player strategy options to a a user, and calls othello to play a
game.
*/
void playgame (void) {
    int i, p1, p2, printflag;
    int (* strfn1)(int, int *); int (* strfn2)(int, int *);
    char * strnme;
        /* get strategy for player 1 (black) from user */
        i=0;
```

```
    printf("Player 1: ");
    while (STRATEGIES[i][0] != NULL) {
            strnme=STRATEGIES[i][1]; printf("%d (%s)\n", i, strnme);
            printf(" ");
            i++;
    }
    printf(": ");
    scanf('%d", &p1);
    /* get strategy for player 2 (white) from user */
    i=0;
    printf("Player 2: ");
    while (STRATEGIES[i][0] != NULL) {
        strnme=STRATEGIES[i][1]; printf("%d (%s)\n", i, strnme);
        printf(" ");
        i++;
    }
    printf(": ");
    scanf("%d", &p2);
    strfn1 = STRATEGIES[p1][2]; strfn2 = STRATEGIES[p2][2];
    if (strfn1 == human || strfn2 == human) printflag = 1;
    else {
        printf(" \n");
        printf("Neither player is human. Do you want to print each board
(1) or not (0): ");
    scanf("%d", &printflag);
    }
    othello(strfn1, strfn2, printflag);
}
/
**********************************************************************
**
******************************** MAIN
***********************************
**********************************************************************
**/
int main (void) {
    do {
        playgame();
        fflush(stdin);
        printf("Do you want to play another game (y or n)? ");
        } while (getchar() == 'y');
/* roundrobin(); /* You will uncomment and run roundrobin to test
```

your alphabeta pruning modifications of minmax, maxchoice and minchoice. */
\}
/* Become familiar with Othello by running the code as written and selecting the following single game options

1) maxdiffstrategy, 1-move lookahead (3) for BLACK against maxweighteddiffstrategy, 1-move lookahead (6) for WHITE

12345678 [b=13 w=0]
10 . . . . . . . .
20 . . . . . . . .
30 . b b b b b . .
40 . . . b b b . .
50 . . . b b b . .
60 . . . . . b . .
70 . . . . . . b .
80 . . . . . . . .
2) maxdiffstrategy, 1-move lookahead (3) for BLACK against maxweighteddiffstrategy, 5-move lookahead (8) for WHITE

12345678 [b=27 w=37]
10 w w w w w w w w
20 b b w w w w w w
30 b b b w w b b b
40 b b b w b w b b
50 b b w b w w w w
60 b w b b w w b w
70 b w w w b b b b
80 b w w w w w w w

What is interesting about this last game is that BLACK leads by a large number of squares until near the very end of the game. Remember that in this latter game, white is doing 5 ply lookahead and is generating something on the order of 2.5 million boards per game (look at the diff/1 vs. wdiff/5 line below under roundrobin results). Thus, expect a delay (a tolerable delay) each time that white moves in this latter game.

If you run roundrobin with the current code (minmax with no pruning), then be prepared to wait quite a while. The following will eventually materialize (which I have indented for a bit better readability):
random wins=1 boards=0
|| diff/1 wins=9 boards=1824
random wins=2 boards=0
|| diff/3 wins=8 boards=174938
random wins=0 boards=0
random wins=3 boards=0
random wins=1 boards=0
random wins=0 boards=0
diff/1 wins=0 boards=1799
diff/1 wins=0 boards=1763
diff/1 wins=4 boards=2134
diff/1 wins=2 boards=2038
diff/1 wins=0 boards=1736
diff/3 wins=3 boards=200450
diff/3 wins=3 boards=202781
diff/3 wins=1 boards=208165
diff/3 wins=1 boards=174285
diff/5 wins=2 boards=18595500
diff/5 wins=4 boards=19102429
diff/5 wins=0 boards=16349918
wdiff/1 wins=0 boards=2311
wdiff/1 wins=1 boards=1944
wdiff/3 wins=1 boards=234330
| diff/5 wins=10 boards=14970716
|| wdiff/1 wins=7 boards=2455
|| wdiff/3 wins=9 boards=293989
wdiff/5 wins=10 boards=33035881
diff/3 wins=10 boards=155657
diff/5 wins=10 boards=16361232
wdiff/1 wins=6 boards=2397
wdiff/3 wins=7 boards=268585
wdiff/5 wins=10 boards=24682590
diff/5 wins=6 boards=19828063
wdiff/1 wins=7 boards=2301
wdiff/3 wins=9 boards=242318
wdiff/5 wins=9 boards=26257282
wdiff/1 wins=8 boards=2383
wdiff/3 wins=5 boards=202807
wdiff/5 wins=10 boards=22520544
wdiff/3 wins=10 boards=292058
wdiff/5 wins=9 boards=29422051
wdiff/5 wins=8 boards=28452315

Each line above shows the results of 10 matches against two strategies.
For example, the last line shows the results of the strategy using 3-ply lookahead with weighteddiffeval (wdiff/3) as the utility function
against 5-ply lookahead with the same utility function (wdiff/5). Over 10 games, wdiff/5 wins 8 , wdiff/3 wins 1 , and there is one tie. Over 10 games, wdiff/5 (in this last case) generates $28,452,315$ boards (or an average of $2,845,232$ boards generated per game)!

If and when you were to implement an incomplete (local) alphabeta pruning running, the results will be something like:
random wins=1 boards=0 random wins=2 boards=0 random wins=0 boards=0 random wins=3 boards=0 random wins=1 boards=0 random wins=0 boards=0 diff1 wins=0 boards=1799 diff1 wins=0 boards=1763 diff1 wins=4 boards=2134 diff1 wins=2 boards=2038 diff1 wins=0 boards=1736 diff3 wins=3 boards=59175 diff3 wins=3 boards=51624
diff3 wins=1 boards=58869
diff3 wins=1 boards=48521

```
|| diff1 wins=9 boards=1824
|| diff3 wins=8 boards=44887
|| diff5 wins=10 boards=944422
|| wdiff1 wins=7 boards=2455
|| wdiff3 wins=9 boards=97418
|| wdiff5 wins=10 boards=2839502
|| diff3 wins=10 boards=44741
|| diff5 wins=10 boards=1038063
|| wdiff1 wins=6 boards=2397
|| wdiff3 wins=7 boards=90605
|| wdiff5 wins=10 boards=2643711
|| diff5 wins=6 boards=1160722
|| wdiff1 wins=7 boards=2301
|| wdiff3 wins=9 boards=84970
|| wdiff5 wins=9 boards=2947041
```

```
diff5 wins=2 boards=1142881 || wdiff1 wins=8 boards=2383
diff5 wins=4 boards=1063738 || wdiff3 wins=5 boards=76715
diff5 wins=0 boards=1124236 || wdiff5 wins=10 boards=2683518
wdiff1 wins=0 boards=2311 || wdiff3 wins=10 boards=89526
wdiff1 wins=1 boards=1944 || wdiff5 wins=9 boards=2635355
wdiff3 wins=1 boards=80708 || wdiff5 wins=8 boards=2844060
```

Notice that the win/loss results do not change at all (minmax with alphabeta pruning chooses exactly the same moves as minmax without alphabeta pruning), but the number of generated boards is vastly reduced. For example, when wdiff5 is pitted against wdiff3, wdiff5 with pruning generates $2,844,060$ boards over 10 games or an average of 284,406 boards per game, as opposed to about 10 times this without pruning.

Results immediately above are from incomplete alpha-beta pruning that we discussed in class. If you are careful to select the full alpha beta procedure (also discussed in class) that is in the text, here is a list of results that you might expect. This version communicates the best and worst move scores (alpha and beta) across multiple levels of the minmax search. In contrast, the incomplete version of alphabeta only communicated the alpha and beta values (best or worst scores discovered
so far) to the immediate children of a node. Note that the results below indicate a further decrease in number of boards expanded (e.g., an average of 201,482 boards per game, down from 284,406, for wdiff5
when pitted against wdiff3)

Full alpha beta (no randomization of moves)
random wins=1 boards=0
random wins=2 boards=0 random wins=0 boards=0 random wins=3 boards=0 random wins=1 boards=0 random wins=0 boards=0 diff1 wins=0 boards=1799 diff1 wins=0 boards=1763 diff1 wins=4 boards=2134 diff1 wins=2 boards=2038 diff1 wins=0 boards=1736 diff3 wins=3 boards=59128 diff3 wins=3 boards=51592
diff3 wins=1 boards=58855
diff3 wins=1 boards=48473
diff5 wins=2 boards=815805
diff5 wins=4 boards=751811

```
    || diff1 wins=9 boards=1824
    || diff3 wins=8 boards=44806
    || diff5 wins=10 boards=693398
    || wdiff1 wins=7 boards=2455
    || wdiff3 wins=9 boards=97374
    || wdiff5 wins=10 boards=1933766
    || diff3 wins=10 boards=44674
    || diff5 wins=10 boards=740534
    || wdiff1 wins=6 boards=2397
    || wdiff3 wins=7 boards=90545
    || wdiff5 wins=10 boards=1871014
    || diff5 wins=6 boards=833302
    || wdiff1 wins=7 boards=2301
    || wdiff3 wins=9 boards=84937
    || wdiff5 wins=9 boards=2072212
    || wdiff1 wins=8 boards=2383
    || wdiff3 wins=5 boards=76700
```

diff5 wins=0 boards=811652
wdiff1 wins=0 boards=2311
wdiff1 wins=1 boards=1944
wdiff3 wins=1 boards=80707
|| wdiff5 wins=10 boards=1910016
|| wdiff3 wins=10 boards=89485
|| wdiff5 wins=9 boards=1823471
wdiff5 wins=8 boards=2014816

When you randomly select amongst the best moves in the minmax function, you can expect different results than the above. In general, this may represent a modest degradation in performance (in terms of Win/Loss for what we regard as the better player) as well as number of boards expanded. This degradation may be an artifact of the randomization process and the fact that we are only playing 10 games per pairs of players in the roundrobin tournament, but there may also be a more systematic bias at work here, which we will discuss.

Full alpha beta (with random selection among the best moves)
random wins=6 boards=0 random wins=3 boards=0 random wins=0 boards=0 random wins=3 boards=0 random wins=1 boards=0 random wins=0 boards=0 diff1 wins=2 boards=2224 diff1 wins=3 boards=2091 diff1 wins=2 boards=2169 diff1 wins=0 boards=1920 diff1 wins=1 boards=1742 diff3 wins=4 boards=74811 diff3 wins=4 boards=56395 diff3 wins=1 boards=63171 diff3 wins=0 boards=53204 diff5 wins=3 boards=1104430 diff5 wins=4 boards=1382107 diff5 wins=1 boards=831579 wdiff1 wins=2 boards=2401 wdiff1 wins=4 boards=2239 wdiff3 wins=1 boards=80897
| diff1 wins=3 boards=1769
|| diff3 wins=7 boards=49151
|| diff5 wins=10 boards=732213
|| wdiff1 wins=7 boards=2444
|| wdiff3 wins=9 boards=96911
| wdiff5 wins=10 boards=1735804
| diff3 wins=8 boards=63567
| diff5 wins=6 boards=731774
| wdiff1 wins=8 boards=2624
| wdiff3 wins=10 boards=85564
| wdiff5 wins=9 boards=2108210
| diff5 wins=6 boards=1094075
wdiff1 wins=6 boards=2503
wdiff3 wins=8 boards=97417
wdiff5 wins=10 boards=2039680
wdiff1 wins=7 boards=2566
wdiff3 wins=3 boards=100405
wdiff5 wins=9 boards=1734347
| wdiff3 wins=7 boards=82616
|| wdiff5 wins=6 boards=2173090
|| wdiff5 wins=9 boards=2114608

